

**Q4-Review B**

Evaluate the logarithmic expression without using a calculator.

1.  $\log_2 32 = x$

$$2^x = 32$$

$$\boxed{x = 5}$$

2.  $\log \sqrt[3]{10}$

$$\log_{10} 10^{1/3}$$

$$\boxed{\frac{1}{3}}$$

3.  $\log_3 1 = x$

$$3^x = 1$$

$$\boxed{x = 0}$$

4.  $\ln e^{-4}$

$$\boxed{-4}$$

5.  $\log_2 0 = x$

$$2^x = 0$$

$$\boxed{\text{no solution}}$$

6.  $\log_3 \left(\frac{1}{9}\right)$

$$\log_3 3^{-2}$$

$$\boxed{-2}$$

Solve the equation.

7.  $10^x = 3$

$$\log_{10} 10^x = \log_{10} 3$$

$$\boxed{x = \log 3}$$

8.  $e^x = 0.75$

$$\ln e^x = \ln 0.75$$

$$\boxed{x = \ln 0.75}$$

9.  $1.07^x = 5$

$$\ln 1.07^x = \ln 5$$

$$x \ln 1.07 = \ln 5$$

$$\boxed{x = \frac{\ln 5}{\ln 1.07}}$$

10.  $\ln x = 3.2$

$$e^{\ln x} = e^{3.2}$$

$$\boxed{x = e^{3.2}}$$

11.  $\log_{10} x = -4$

$$\boxed{x = 10^{-4}}$$

12.  $2^{x-3} = 5$

$$\log 2^{x-3} = \log 5$$

$$(x-3) \log 2 = \log 5$$

$$x-3 = \frac{\log 5}{\log 2}$$

$$\boxed{x = \frac{\log 5}{\log 2} + 3}$$

13.  $2 \log_3 x + 1 = 5$

$$2 \log_3 x = 4$$

$$\log_3 x = 2$$

$$x = 3^2$$

$$\boxed{x = 9}$$

14.  $\log(x+2) + \log(x-1) = 1$

$$\log_{10}((x+2)(x-1)) = 1$$

$$\log_{10}(x^2 + x - 2) = 1$$

$$x^2 + x - 2 = 10$$

$$x^2 + x - 12 = 0$$

$$(x+4)(x-3)$$

$$\boxed{x = -4, 3}$$

15.  $\ln(3x+4) - \ln 2 = 5$

$$e^{\ln\left(\frac{3x+4}{2}\right)} = e^5$$

$$\frac{3x+4}{2} = e^5$$

$$3x+4 = 2e^5$$

$$\boxed{x = \frac{2e^5 - 4}{3}}$$

Use the properties of logarithms to write as a single logarithm.

16.  $\log x + \log 5$

$$\boxed{\log 5x}$$

17.  $4\log y - \log z$

$$\log y^4 - \log z$$

$$\boxed{\log \frac{y^4}{z}}$$

18.  $3\ln(x^3y) + 2\ln(yz^2)$

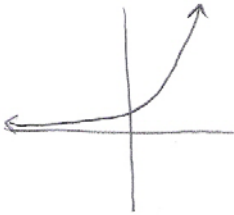
$$\ln(x^3y)^3 + \ln(yz^2)^2$$

$$\ln(x^9y^3 \cdot y^2z^4)$$

$$\boxed{\ln(x^9y^5z^4)}$$

Graph each function without using a calculator.

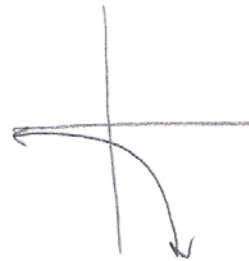
19.  $y = e^x$



20.  $y = \ln x$



21.  $y = -e^x$



22.  $y = \ln(x-4)$

