

Solve the following rational expressions.

3.

$$\frac{3}{x+2} - \frac{1}{x} = \frac{1}{5x}$$

$$\left(\frac{3}{x+2} - \frac{1}{x} = \frac{1}{5x}\right) (5x(x+2))$$

$$3(5x) - (5(x+2)) = 1(x+2)$$

$$15x - 5x - 10 = x + 2$$

$$10x - 10 = x + 2$$

$$9x = 12$$

$$x = \frac{12}{9}$$

$$x = \frac{4}{3}$$

What is the **least common denominator**? $5x(x+2)$

What are the **excluded values**?

$$\frac{x = -2}{x = 0}$$

Solution(s): $x = \frac{4}{3}$

4.

$$\frac{1}{x+3} + \frac{2}{x} = \frac{-3}{x(x+3)}$$

$$\left(\frac{1}{x+3} + \frac{2}{x} = \frac{-3}{x(x+3)}\right) (x(x+3))$$

$$x + 2(x+3) = -3$$

$$x + 2x + 6 = -3$$

$$3x = -9$$

$$x = -3$$

What is the **least common denominator**? $x(x+3)$

What are the **excluded values**?

$$\frac{x = 0}{x = -3}$$

Solution(s): NO SOLUTION

5.

$$\frac{1}{x-6} + \frac{x}{x-2} = \frac{4}{x^2 - 8x + 12}$$

$$\left(\frac{1}{x-6} + \frac{x}{x-2} = \frac{4}{(x-2)(x-6)}\right) (x-2)(x-6)$$

$$1(x-2) + x(x-6) = 4$$

$$x-2 + x^2 - 6x = 4$$

$$x^2 - 5x - 6 = 0$$

$$(x-6)(x+1) = 0$$

$$x = 6 \quad x = -1$$

What is the **least common denominator**? $(x-2)(x-6)$

What are the **excluded values**?

$$\frac{x = 2}{x = 6}$$

Solution(s): $x = -1$