

Graphing quadratics in standard form:

Standard Form: $y = ax^2 + bx + c$

Rewrite in vertex form by completing the square.

Example 3: Rewrite each quadratic in vertex form then graph.

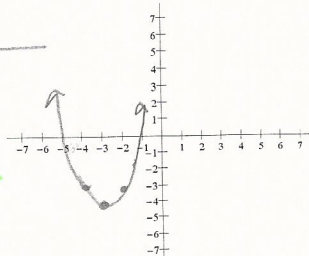
a) $y = x^2 + 6x + 5$

$$y = (x^2 + 6x + \underline{\quad}) + 5 - \underline{\quad}$$

$$\left(\frac{6}{2}\right) = \underline{3} \quad (3)^2 = \underline{9}$$

$$y = (x^2 + 6x + \underline{9}) + 5 - \underline{9}$$

$$y = (x + \underline{3})^2 - 4$$



vertex: $(\underline{-3}, \underline{-4})$

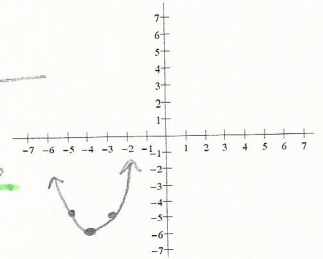
b) $y = x^2 + 8x + 10$

$$y = (x^2 + 8x + \underline{\quad}) + 10 - \underline{\quad}$$

$$\frac{8}{2} = \underline{4} \quad (4)^2 = \underline{16}$$

$$y = (x^2 + 8x + \underline{16}) + 10 - \underline{16}$$

$$y = (x + \underline{4})^2 - 6$$



vertex: $(\underline{-4}, \underline{-6})$

c) $y = 3x^2 - 12x + 24$

$$y = (3x^2 - 12x + \underline{\quad}) + 24 - \underline{\quad}$$

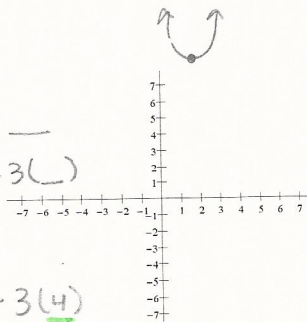
$$y = 3(x^2 - 4x + \underline{\quad}) + 24 - 3(\underline{\quad})$$

$$-\frac{4}{2} = \underline{-2} \quad (2)^2 = \underline{4}$$

$$y = 3(x^2 - 4x + \underline{4}) + 24 - 3(\underline{4})$$

$$y = 3(x - \underline{2})^2 + 12$$

vertex: $(\underline{2}, \underline{12})$



d) $y = -2x^2 + 12x - 13$

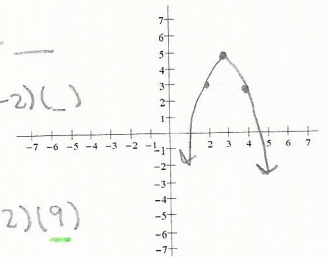
$$y = (-2x^2 + 12x + \underline{\quad}) - 13 - \underline{\quad}$$

$$y = -2(x^2 - 6x + \underline{\quad}) - 13 - (-2)(\underline{\quad})$$

$$-\frac{6}{2} = \underline{-3} \quad (-3)^2 = \underline{9}$$

$$y = -2(x^2 - 6x + \underline{9}) - 13 - (-2)(\underline{9})$$

$$y = -2(x - \underline{3})^2 + 5$$



vertex: $(\underline{3}, \underline{5})$

Writing Equations of Lines

Point-Slope Form: $y = m(x - x_1) + y_1$

$m = \text{slope}$

x_1 and y_1 are from the point that is given to you. (x_1, y_1)

Example 4: Use the given information to write the equation of each line.

a) point $(4, -3)$, slope = 2

$$y = 2(x - 4) + (-3)$$

$$y = 2x - 8 - 3$$

$$y = 2x - 11$$

b) point $(-3, -2)$, slope = $\frac{1}{2}$

$$y = \frac{1}{2}(x - (-3)) + (-2)$$

$$y = \frac{1}{2}(x + 3) - 2$$

$$y = \frac{1}{2}x + \frac{3}{2} - 2$$

$$y = \frac{1}{2}x - \frac{1}{2}$$

c) point $(0, 3)$ and $(-2, 7)$

$$m = \frac{7-3}{-2-0} = \frac{4}{-2} = -2$$

* use point $(0, 3)$

$$y = -2(x - 0) + 3$$

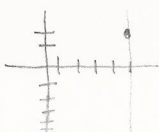
$$y = -2x + 3$$

d) point $(5, -8)$ and $(5, 2)$

$$m = \frac{-8-2}{5-5} = \frac{-10}{0}$$

slope is undefined.

$$x = 5$$



e) point $(3, -1)$,

parallel to the line $y = \frac{4}{3}x + 7$ $m = 4$

$$m = 4$$

$$y = 4(x - 3) + (-1)$$

$$y = 4x - 12 - 1$$

$$y = 4x - 13$$

f) point $(0, 5)$

perpendicular to the line $y = \frac{4}{3}x + 7$ $m = 4$

$$m = -\frac{1}{4}$$

$$y = -\frac{1}{4}(x - 0) + 5$$

$$y = -\frac{1}{4}x + 5$$

Factoring

Example 1: Factor out a common monomial

a) $5x^4 + 10x^3 + 25x$
GCF: $5x$

$$5x(x^3 + 2x^2 + 5)$$

b) $6x^4 + 21x^2$
GCF: $3x^2$

$$3x^2(2x^2 + 7)$$

c) $-2x^3 + 8x^2 - 18x$
GCF: $-2x$

$$-2x(x^2 - 4x + 9)$$

Example 2: Factor using guess and check. Recall: $ax^2 + bx + c$

a) $x^2 + 9x + 18$ $\begin{array}{r} 18 \quad 9 \\ 6, 3 \quad 9 \end{array}$

$$\begin{array}{c} \curvearrowright \quad \curvearrowleft \\ x^2 + 6x + 3x + 18 \end{array}$$

$$x(x+6) + 3(x+6)$$

$$(x+6)(x+3)$$

b) $x^2 - x - 6$ $\begin{array}{r} -6 \quad -1 \\ -3, 2 \quad -1 \end{array}$

$$\begin{array}{c} \curvearrowright \quad \curvearrowleft \\ x^2 - 3x + 2x - 6 \end{array}$$

$$x(x-3) + 2(x-3)$$

$$(x-3)(x+2)$$

c) $2x^2 - 5x - 3$ $a \cdot c = 2(-3) = -6$

$$\begin{array}{c} -6 \quad -5 \\ -6, 1 \quad -5 \end{array}$$

$$2x^2 - 6x + x - 3$$

$$2x(x-3) + 1(x-3)$$

$$= (x-3)(2x+1)$$

d) $6x^2 - 13x + 2$ $a \cdot c = 6(2) = 12$ $\begin{array}{r} 12 \quad -13 \\ -12, -1 \quad -13 \end{array}$

$$\begin{array}{c} 6x^2 - 12x - x + 2 \\ 6x(x-2) + 1(x-2) \end{array}$$

$$= (x-2)(6x+1)$$

e) $2x^2 + 7x - 4$ $a \cdot c = 2(-4) = -8$ $\begin{array}{r} -8 \quad 7 \\ 8, -1 \quad 7 \end{array}$

$$\begin{array}{c} 2x^2 + 8x - x - 4 \\ 2x(x+4) - 1(x+4) \end{array}$$

$$= (x+4)(2x-1)$$

f) $10x^2 + 7x - 12$ $a \cdot c = 10(-12) = -120$ $\begin{array}{r} -120 \quad 7 \\ 15, -8 \quad 7 \end{array}$

$$\begin{array}{c} 10x^2 + 15x - 8x - 12 \\ 5x(2x+3) - 4(2x+3) \end{array}$$

$$= (2x+3)(5x-4)$$

Example 3: Factor by grouping.

a) $x^3 + 4x^2 + 5x + 20$

$$x^2(x+4) + 5(x+4)$$

$$= (x+4)(x^2+5)$$

b) $8x^3 + 2x^2 - 12x - 3$

$$2x^2(4x+1) - 3(4x+1)$$

$$= (4x+1)(2x^2-3)$$

c) $2x^3 + 3x^2 - 8x - 12$

$$x^2(2x+3) - 4(2x+3)$$

← difference of squares
 $a^2 - b^2 = (a-b)(a+b)$

$$= (2x+3)(x^2-4)$$

$$= (2x+3)(x-2)(x+2)$$

Solve Equations Graphically:

1. When equal to zero:

$$ax^2 + bx + c = 0$$

• use the graph to find the x-intercepts (or zeros)

2. When variables are on both sides:

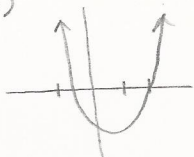
$$ax^2 + b = dx^3 + c$$

• graph $y_1 = ax^2 + b$ and $y_2 = dx^3 + c$ and find where the lines intersect.

Example 1: Solve each equation graphically.

a) $2x^2 - 3x - 2 = 0$

• use the calculator to graph $y = 2x^2 - 3x - 2$ and find the x-intercepts (zeros)



$$x = -\frac{1}{2}, x = 2$$

b) $6c + 4 = c^3 + 5c - 1$

• use $y_1 = 6x + 4$ and $y_2 = x^3 + 5x - 1$. Find where the graphs intersect.

$$x \approx 1.9042$$

c) $|2x - 1| = 6$

• use $y_1 = |2x - 1|$ and $y_2 = 6$. Find where the graphs intersect.

$$x = -\frac{5}{2}, x = \frac{7}{2}$$