

UNIT 2 QUIZ REVIEW

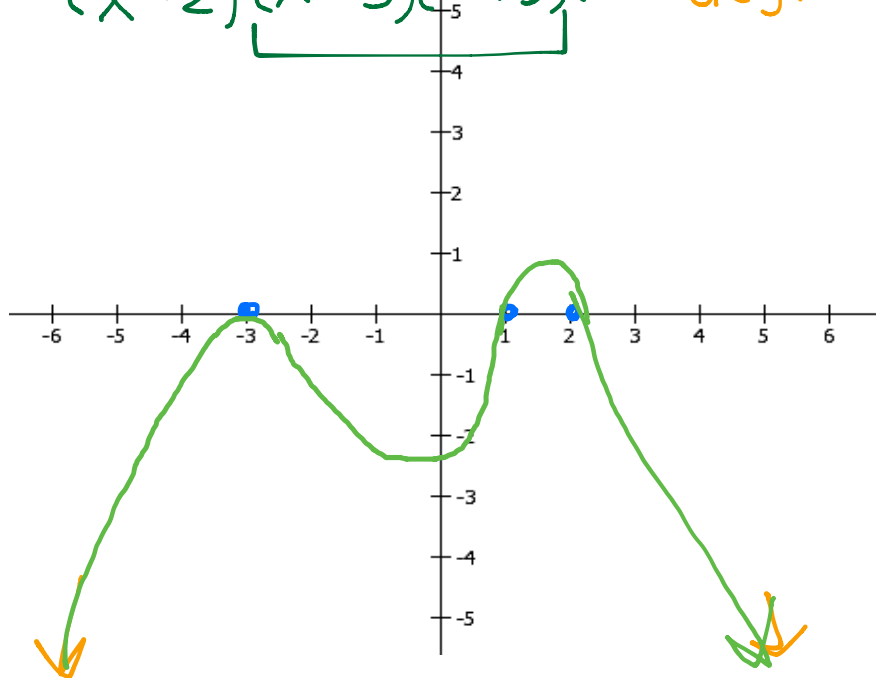
Polynomials

Use the zeros and end behavior of the polynomial to sketch a graph of each function.

$$y = -(x - 2)^1(x + 3)^2(x - 1)^1$$

$-(x - 2)(x + 3)(x + 3)(x - 1)$ degree: 4 l.c.: -

zeros:
 $x = 2$ (cross)
 $x = -3$ (touch)
 $x = 1$ (cross)



Find all the possible rational zeros

$$f(x) = 5x^4 - 11x^2 + 6$$

$$\frac{p}{q} : \frac{\pm 1, \pm 2, \pm 3, \pm 6}{\pm 1, \pm 5}$$

possible rational zeros: $\pm 1, \pm \frac{1}{5}, \pm 2, \pm \frac{2}{5}, \pm 3, \pm \frac{3}{5}, \pm 6, \pm \frac{6}{5}$

Find all complex zeros (real and imaginary if they exist) of each polynomial.

$$f(x) = x^5 - 2x^4 - x^3 + 8x^2 - 10x + 4$$

$$\frac{p}{q}: \frac{\pm 1, \pm 2, \pm 4}{\pm 1}$$

$$\begin{array}{r|rrrrrr} 1 & 1 & -2 & -1 & 8 & -10 & 4 \\ & \downarrow & & & & & \\ \hline & 1 & -1 & -2 & 6 & -4 & 0 \end{array}$$

$$\begin{array}{r|rrrrr} -2 & 1 & -1 & -2 & 6 & -4 \\ & \downarrow & & & & \\ \hline & 1 & -3 & 4 & -2 & 0 \end{array}$$

$$\begin{array}{r|rrrr} 1 & 1 & -3 & 4 & -2 \\ & \downarrow & & & \\ \hline & 1 & -2 & 2 & 0 \end{array}$$

$$x^2 - 2x + 2$$

$$x = \frac{2 \pm \sqrt{4 - 4(1)(2)}}{2}$$

$$x = \frac{2 \pm \sqrt{-4}}{2}$$

$$x = \frac{2 \pm 2i}{2} = 1 \pm i$$

Zeros:

$$x = 1, x = -2, x = 1, x = 1 \pm i$$

Find all complex zeros (real and imaginary if they exist) of each polynomial.

$$f(x) = x^3 - 3x^2 - 10x + 24$$

$$p: \pm 1, \pm 2, \pm 3, \pm 4, \pm 6, \pm 8, \pm 12, \pm 24$$
$$q: \pm 1$$

$$\begin{array}{r|rrrr} 2 & 1 & -3 & -10 & 24 \\ & \downarrow & 2 & -2 & -24 \\ \hline & 1 & -1 & -12 & 0 \end{array}$$

$$x^2 - x - 12 = 0$$

$$(x - 4)(x + 3) = 0$$

$$x = 4 \quad x = -3$$

$$\text{zeros: } x = 2, x = 4, x = -3$$

Rewrite the polynomial in factored form

$$f(x) = x^4 - 4x^3 + 3x^2 + 2x - 6$$

$$\frac{p}{q}: \frac{\pm 1, \pm 2, \pm 3, \pm 6}{\pm 1}$$

$$\begin{array}{r} \textcircled{-1} \\ \underline{} \\ \begin{array}{r} 1 \quad -4 \quad 3 \quad 2 \quad -6 \\ \downarrow \quad -1 \quad 5 \quad -8 \quad 6 \\ \hline 1 \quad -5 \quad 8 \quad -6 \quad | \quad 0 \end{array} \end{array}$$

$$f(x) = (x+1)(x-3)(\underline{x^2-2x+2})$$

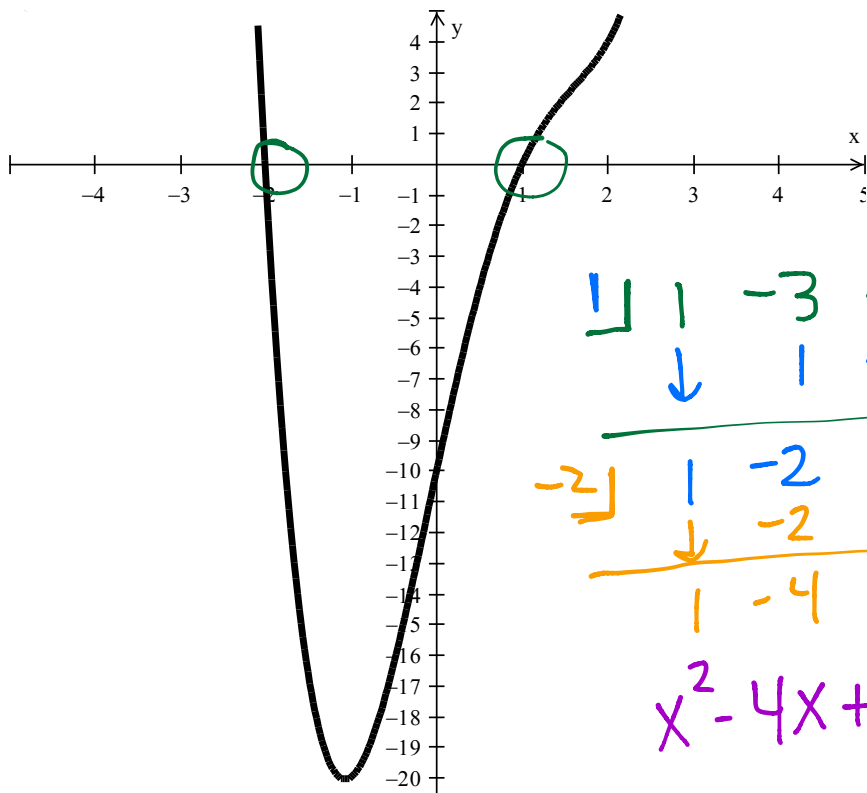
$$\begin{array}{r} \textcircled{3} \\ \underline{} \\ \begin{array}{r} 1 \quad -5 \quad 8 \quad -6 \\ \downarrow \quad 3 \quad -6 \quad 6 \\ \hline 1 \quad -2 \quad 2 \quad | \quad 0 \end{array} \end{array}$$

$$x^2 - 2x + 2$$

Use the graph to find the zeros of $f(x)$.

Show work

$$f(x) = x^4 - 3x^3 - x^2 + 13x - 10$$



$$x = \frac{4 \pm \sqrt{16 - 4(1)(5)}}{2}$$
$$x = \frac{4 \pm \sqrt{-4}}{2}$$
$$x = \frac{4 \pm 2i}{2}$$
$$x = 2 \pm i$$

$$\begin{array}{r} \downarrow \\ 1 \quad -3 \quad -1 \quad 13 \quad -10 \\ \downarrow \quad 1 \quad -2 \quad 3 \quad 10 \\ \hline 1 \quad -2 \quad -3 \quad 10 \quad 0 \\ -2 \downarrow \quad -2 \quad 8 \quad -10 \\ \hline 1 \quad -4 \quad 5 \quad 0 \end{array}$$

$$x^2 - 4x + 5$$

Zeros: $x = 1, x = -2$
 $x = 2 \pm i$

Write a polynomial in **standard form**

degree: 4; zeros: -2, 3/2, -1 multiplicity 2;

leading coefficient: 2

$$(x+2)(2x-3)(x+1)(x+1) \quad \text{FOIL}$$

$$(2x^2 + x - 6)(x^2 + 2x + 1)$$

$$= 2x^4 + \underline{4x^3} + \underline{2x^2} + \underline{x^3} + \underline{2x^2} + \underline{x} - \underline{6x^2} - \underline{12x} - \underline{6}$$

$$= \boxed{2x^4 + 5x^3 - 2x^2 - 11x - 6}$$

Write a polynomial in **standard form**

degree: 3; zeros: $-3, -1+i, -1-i$

leading coefficient of 1

$$\begin{aligned} & (x+3)(x+1+i)(x+1-i) \\ &= (x+3)(x^2 + x - ix + x + 1 - i + ix + i - i^2) \\ &= (x+3)(x^2 + 2x + 2) \\ &= (x^3 + 2x^2 + 2x + 3x^2 + 6x + 6) \\ &= \boxed{x^3 + 5x^2 + 8x + 6} \end{aligned}$$

Use the given zero to find all remaining zeros.

$$f(x) = 5x^5 + 9x^4 + 3x^3 - 11x^2 - 8x + 2$$

Given $-1 + i, -1 - i$

$$(x+1+i)(x+1-i) = x^2 + 2x + 2$$

$$\begin{array}{r}
 \overline{5x^3 - x^2 - 5x + 1} \\
 x^2 + 2x + 2 \overline{) 5x^5 + 9x^4 + 3x^3 - 11x^2 - 8x + 2} \\
 \underline{- 5x^5 + 10x^4 + 10x^3} \\
 0 -x^4 - 7x^3 - 11x^2 \\
 \underline{+ x^4 + 2x^3 + 2x^2} \\
 -5x^3 - 9x^2 - 8x \\
 \underline{+ 5x^3 + 10x^2 + 10x} \\
 0x^3 + x^2 + 2x \\
 \underline{+ x^2 + 2x + 2} \\
 0
 \end{array}$$

$$x^2 + 2x + 2$$

$$5x^3 - x^2 - 5x + 1$$

$$x^2(5x-1) - 1(5x-1)$$

$$(5x-1)(x^2-1) = 0$$

$$x = \frac{1}{5} \quad x = 1 \quad x = -1$$